

# Mathematics for Safe AI

## **Opportunity space**

v1.0

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### CONTEXT

This document describes an opportunity space - an area that we believe is likely to yield breakthroughs, from which one or more funding programmes will emerge.

You can find out more about opportunity seeds within this space <u>here.</u> We have launched a programme in this space, Safeguarded AI – find out more <u>here.</u>

This opportunity space is not currently soliciting feedback – you can stay up to date with this opportunity space, plus others across ARIA, **here**.

An ARIA opportunity space should be

- + important if true (i.e. could lead to a significant new capability for society),
- + under-explored relative to its potential impact, and
- + ripe for new talent, perspectives, or resources to change what's possible.

We don't yet have known technical solutions to ensure that powerful AI systems interact as intended with real-world systems and populations. A combination of scientific world-models and mathematical proofs may be the answer to ensuring AI provides transformational benefit without harm.

#### BELIEFS

The core beliefs that underpin/bound this area of opportunity.

- 1. Future AI systems will be powerful enough to transformatively enhance or threaten human civilisation at a global scale → we need as-yet-unproven technologies to certify that cyber-physical AI systems will deliver intended benefits while avoiding harms.
- Given the potential of AI systems to anticipate and exploit world-states beyond human experience or comprehension, traditional methods of empirical testing will be insufficiently reliable for certification → mathematical proof offers a critical but underexplored foundation for robust verification of AI.
- It will eventually be possible to build mathematically robust, human-auditable models that comprehensively capture the physical phenomena and social affordances that underpin human flourishing → we should begin developing such world models today to advance transformative AI and provide a basis for provable safety.

#### **OBSERVATIONS**

Some signposts as to why we see this area as important, underserved, and ripe.

Al holds the potential to dramatically improve physical health, economic well-being, and human empowerment, on a scale exceeding the industrial revolution—if deployed wisely [1].



#### ENGAGE

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If you require an accessible version of this document and/or form, please contact us at **info@aria.org.uk**.

#### SOURCES

A compiled, but not exhaustive list of works helping to shape our view and frame the opportunity space (for those who want to dig deeper).

- 1. <u>The transformative potential of artificial intelligence</u>
- 2. <u>Provably safe systems: The only path to controllable AGI</u>
- 3. <u>ProofNet: Autoformalizing and formally proving undergraduate-level</u> <u>mathematics</u>
- 4. Llemma: An open language model for mathematics
- 5. <u>Toward verified artificial intelligence</u>
- 6. Formal verification for neural networks via branch-and-bound
- 7. <u>COOL-MC: A comprehensive tool for reinforcement learning and model</u> <u>checking</u>
- 8. <u>Probabilistic model checking and autonomy</u>
- 9. Automated verification and synthesis of stochastic hybrid systems: A survey
- Probabilities are not enough: Formal controller synthesis for stochastic dynamical models with epistemic uncertainty
- 11. <u>Introducing superalignment</u>
- 12. Statement on Al risk
- <u>CEO of AI company warns his tech has a large chance of ending the world</u>
- <u>The CEO of the company behind AI chatbot ChatGPT says worst-case</u>
- scenario for AI is 'lights out for all of us'
- 15. <u>Adversarial strategies beat superhuman go Als</u>
- 16. <u>Plotting progress in Al</u> (Figure 1)
- 17. Some high-level thoughts on the DeepMind alignment team's strategy
- 18. <u>Anthropic's "core views on AI safety"</u>
- 19. SatLM: Satisfiability-aided language models using declarative prompting
- 20. From word models to world models
- 21. VNN-COMP (Verification of Neural Networks COMPetition)
- 22. Evaluation of AlphaFold on stability of missense variations in cancer (Protein structure)
- 23. <u>Magnetic control of tokamak plasmas through deep RL</u>

#### **EXTENDED BIBLIOGRAPHY**

For an even deeper dive...

- 24. Robust control for dynamical systems with non-Gaussian noise via formal abstractions
- 25. Al scientists: Safe and useful AI?
- 26. Towards autoformalization of mathematics and code correctness: Experiments with elementary proofs
- 27. <u>A list of core AI safety problems & how I hope to solve them</u>
- 28. <u>Towards a research program on compositional</u> world-modeling
- 29. <u>Collective constitutional AI: Aligning a language model</u> with public input
- 30. xVal: A continuous number encoding for LLMs
- 31. <u>An overview of catastrophic AI risks</u>
- 32. <u>GFlowNets for AI-driven scientific discovery</u>
- When to trust AI: Advances and challenges for certification of neural networks
- 34. <u>Eureka: Human-level reward design via coding large</u> <u>language models</u>
- 35. <u>Faster sorting algorithms discovered using deep</u> reinforcement learning
- 36. Fairness, accountability, transparency, and ethics (FATE)
- 37. davidad's bold plan for alignment
- Sam Altman, the man behind ChatGPT, is increasingly alarmed about what he unleashed

- 39. Trustworthy autonomous system development
- 40. Misspecification in inverse reinforcement learning
- 41. <u>Experimental results from applying GPT-4 to an</u> <u>unpublished formal language</u>
- 42. Fundamental limitations of alignment in LLMs
- 43. LeanDojo: Theorem proving with retrieval-augmented LLMs
- 44. Language to rewards for robotic skill synthesis
- 45. Democratic inputs to Al
- 46. Neural abstractions
- 47. Individual fairness guarantees for neural networks
- 48. Discovering faster matrix multiplication with RL
- 49. <u>LCRL: Certified policy synthesis via logically-constrained</u> reinforcement learning
- 50. Provably beneficial artificial intelligence
- 51. <u>Goal misgeneralization</u>
- 52. Autoformalization with large language models
- 53. Learning control policies for stochastic systems with reach-avoid guarantees
- 54. Advancing mathematics by guiding human intuition with AI
- 55. The seL4 microkernel: An introduction
- 56. Safety verification of deep neural networks
- 57. The basic AI drives